

Action of a Three Phase
Induction Motor under Various
Forms of Pressure Waves

John Brackett
A. R. Redman

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VARIOUS FORMS of PRESSURE WAVE.

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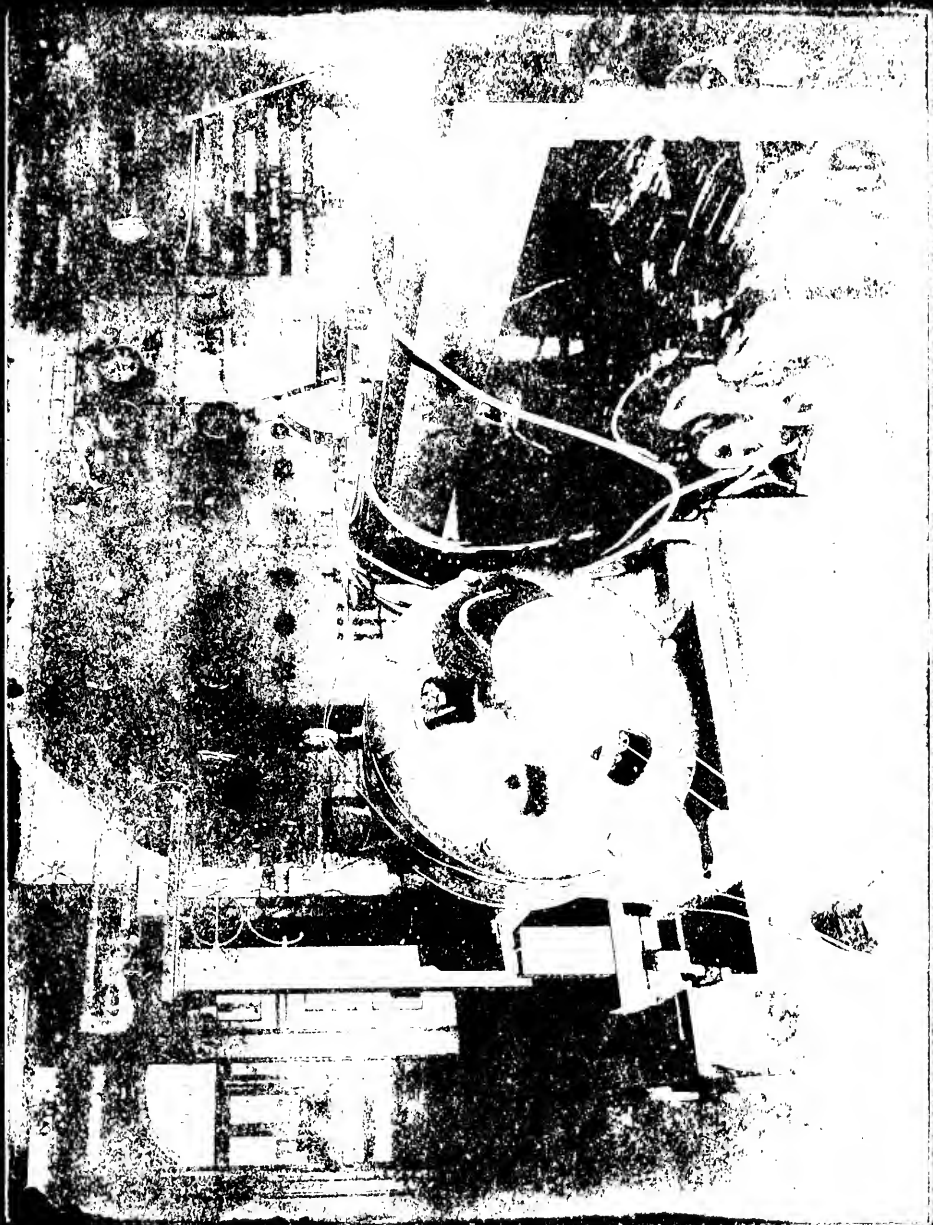
A THESIS
PRESENTED to the TRUSTEES and FACULTY
of the
ARMOUR INSTITUTE of TECHNOLOGY
FOR THE DEGREE OF
BACHELOR OF SCIENCE IN ELECTRICAL ENGINEERING

BY

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John Brackett
J. E. R. Redman

C. E. Freeman
Professor of Electrical Eng.
H. M. Raymond
Dean of Engineering
L. C. Morin
Dean of Cultural Studies



THE ACTION OF A THREE PHASE INDUCTION MOTOR WITH VARIOUS
FORMS OF PRESSURE WAVE.

I N T R O D U C T I O N .

A general study of the effect of wave form upon induction motor performance is not attempted in this discussion, as such an investigation would be impossible with the time and material ordinarily available in a technical course. The object of this paper is to give the results of a few careful tests on a given motor supplied with three phase current by various forms of pressure wave.

The problems met in securing these results were such as to make logical a division of the thesis into two parts:

1st. Securing the wave forms.

2nd. Running the tests.





PART I.

PRODUCTION OF WAVE FORMS.

The principal methods of production of distorted wave forms which suggest themselves are these:

1. "Injecting" capacity, inductance or resistance into the external circuit at various points of the wave
2. Setting up fluctuations in the generator field at similar points.
3. Combination of a fundamental with one or more waves of harmonic frequencies.

The first of these has been used---(See Lond. Elec. 5-15-96), in tests on the iron loss of transformers where small single phase currents were required, but in case of three phase currents of the magnitudes required for starting a squirrel cage motor make the scheme scarcely practicable.

The second method is limited in three phase work by the fact that to retain symmetry of the waves, only certain points may be indented and also because any fluctuations of field which were of sufficient magnitude to effect the wave were found to heat the magnets excessively due to abnormal iron losses in the solid cores of the only machines available.

The third scheme was the one used and in the application of it in seeming obvious manners some rather unlooked for difficulties were encountered.

The fundamental wave was secured from a "Wood" 2-3 phase rotary, 30 K.W., 85 V., 500 R.P.M.. A third harmonic was secured by running at 1500 R.P.M. A general electric type A.T.B., 15 K.W., 85 V., 6 pole, 60 cycles, 6 phase generator. The two were accurately lined and coupled by a Renold silent chain set purchased from the Link Belt Eng. Co., Chicago, and giving a 3-1 reduction. The large gear was mounted on



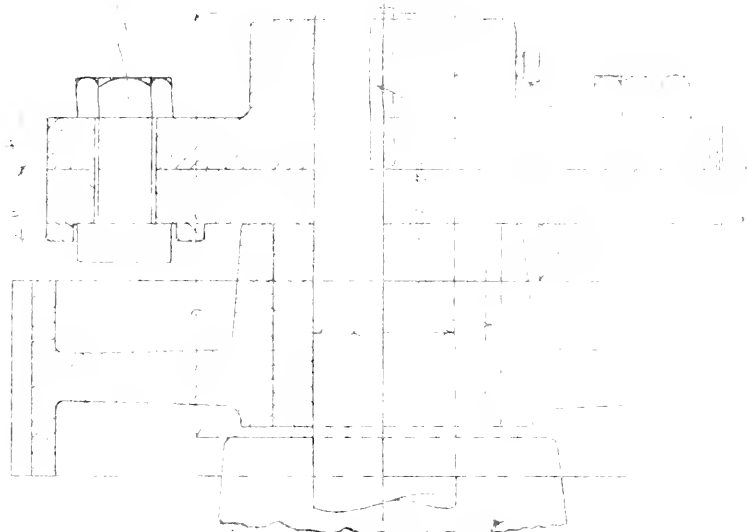
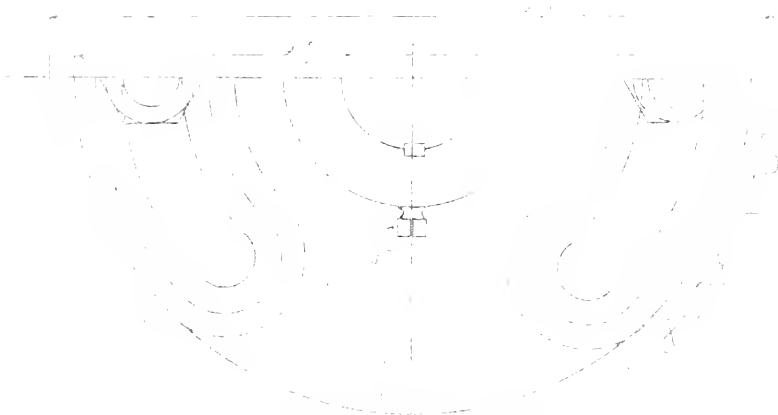
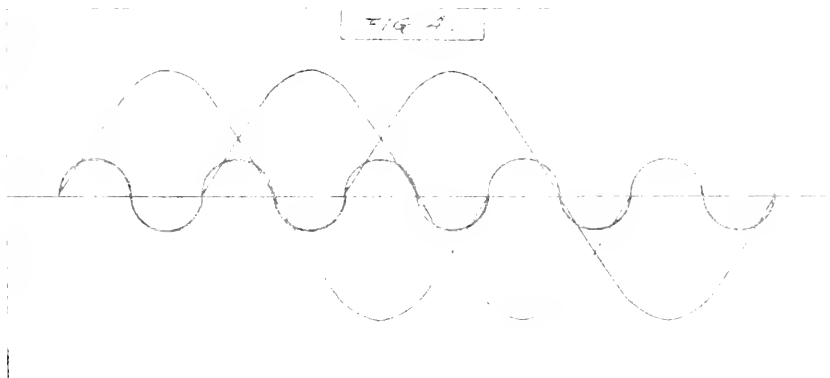


Fig 1



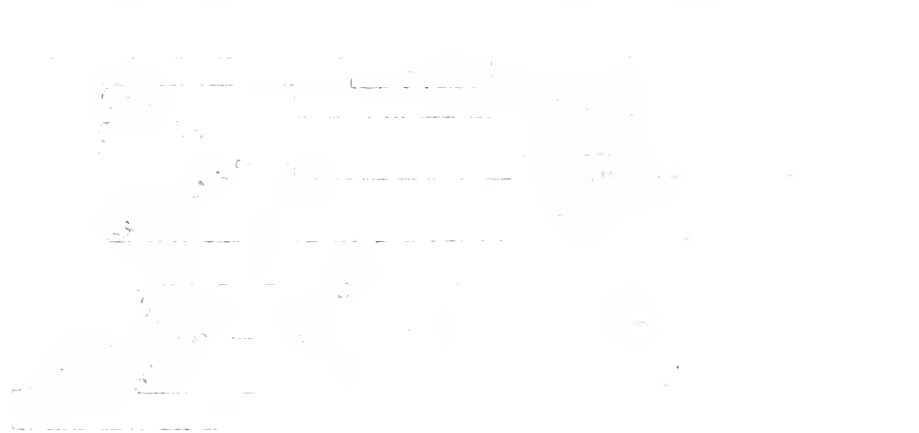
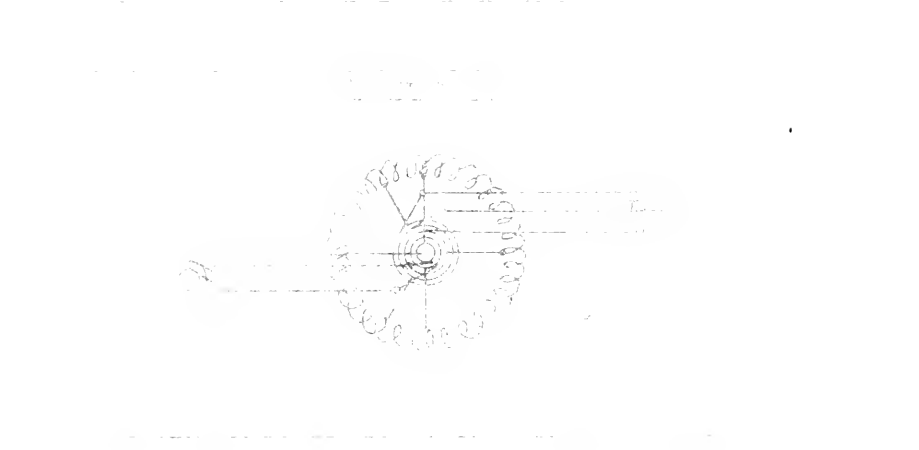


a special flange made in the Institute Shops and designed to give a possible angular displacement of 360 electrical degrees, relatively to the rotary shaft. Fig. 1 shows this flange in detail. So far as the quietness of running of the set even up to 2,000 revolutions it left nothing to be desired.

The curves were traced by means of a contact maker with a movable brush, coupled to the rotary shaft by a flexible joint. The pressure through it was balanced through a telephone against the drop over a portion of a warren "potential rheostat" balance being indicated by the point of minimum sound and the pressure read on Weston, D. C. 0-15, 0-150, Voltmeter, No. 4392, which was checked against Otto Wolf potentiometer No. 440 and found accurate within .5 volts at all parts of the scale. All curves were plotted direct from the voltmeter and contact maker indications, eliminating the taking of data and showing at once any peculiarity of the curve, allowing it to be gone over slowly.

The problem of electrical connections seemed at first glance simple. The 75 cycle generator was given 3 phase connections and a coil placed in each of the rotary leads (Fig. 3). Three dissymmetrical waves were produced. This is explained by the fact that to maintain the same phase relations between each pair of 25 and 75 cycle, or fundamental and harmonic coils, the harmonics should plainly differ in phase by 120 degrees on the fundamental scale, or if the expressions may be used, 120 "fundamental degrees" 120 fundamental degrees corresponds to 120×3 equals 360 third harmonic degrees or degrees on the harmonic scale. Consequently the thirds should differ in phase by 360 degrees, making them identical. In Fig. 4, 3 phases of the fundamental and a single third is plotted. This brings out the point clearly, showing that the 3 phases will be affected in the same way





by a single (or 3 coincident) waves of triple frequency.

To conform to this the low tension sides of 3 phase transformers were put into the rotary leads, and their high tension sides each connected in parallel with that of a fourth transformer excited from a phase of the 75 cycle generator (Fig.5). No distortion of the wave form was produced, the harmonics simply neutralizing each other, a pressure being increased a certain amount going out on one line and cut down the same amount coming back on either of the other two lines. As a method of eliminating this opposition of voltage the harmonic coils were connected inside the delta. As it was impossible to get inside the rotary delta, the rotary pressures were stopped by means of two 3 phase transformers to another delta, the secondary of the final transformer, which could be gotten into Fig. 6, shows this set of connections.

No distortion of wave was produced. This is due to the fact that the 3 harmonic voltages acting in phase set up cross currents around the delta which exactly counter-balance their own pressures. This would be analogous at any instant to a scheme such as Fig. 7, where 3 batteries are connected in the sides of a mesh of resistances as indicated. It can at once be seen that the drops over the resistances would leave the P. D. at the corners of the mesh equal to zero.

To eliminate the cross currents the mesh was opened at a point (Fig.8) killing one leg, but still giving a correct 3 phase circuit. This gave two similar waves, but the third was distorted more than the other two, due to two of the harmonics acting on it in series.

One of the waves was used to run a second 2-3 phase rotary single phase (Fig.9) and waves traced from the 3 phase terminals. They were dissimilar and it began to look as if three similar waves, 120 degrees apart and containing a third could not exist in an interconnected circuit, the thirds

either neutralizing each other in a star, or neutralizing themselves, by a cross current in a mesh.

If three waves of a fifth harmonic frequency be combined with three fundamentals 120 degrees apart, as before, to produce three similar waves, they must differ in phase by 120 fundamentals---120 x 5 equal 600, the equivalent of 120, harmonic degrees. Consequently the objections to the introduction of a third would not hold for a fifth.

It is unfortunate that the time available would not permit a thorough investigation of this interesting point. That the effects of the harmonic are neutralized has been shown clearly above and the means by which it is accomplished seem clear. Indeed in the mesh the actual cross current was measured, and tests with a telephone across the corners of the delta with the full cross current flowing gave only a slight hum, probably due to some unbalance in the impedances of the sides. With the delta open and the cross current thus eliminated waves showing the effect of the third were secured from a circuit which with the delta closed, gave under the same conditions. These similar sine waves.

The matter seems of considerable theoretical interest. Since a coil generating a wave which is the sum of a fundamental and a third may for purposes of discussion be replaced by two coils in series, one generating the fundamental and the other the third, it seems but a short step to suppose that if a wave comprising a third be generated in any delta connected piece of 3 phase apparatus, a rotary for instance, a cross current will be set up, with a corresponding loss of efficiency. A star connection would be subject to the same loss of power, due to opposition of voltages.

This condition is not likely to exist in 3 phase generating apparatus, for it may be shown (Steinmetz "Phenomena", p.389) that due to the slots per pole of a 3 phaser forming a multiple of 3 the third harmonic is not likely to be prominent due to any distortion of flux, the principal cause of such higher harmonics. Steinmetz further shows, however, (page 392) harmonics set up by fluctuations of reactance such as by hysteresis tend strongly to accentuate

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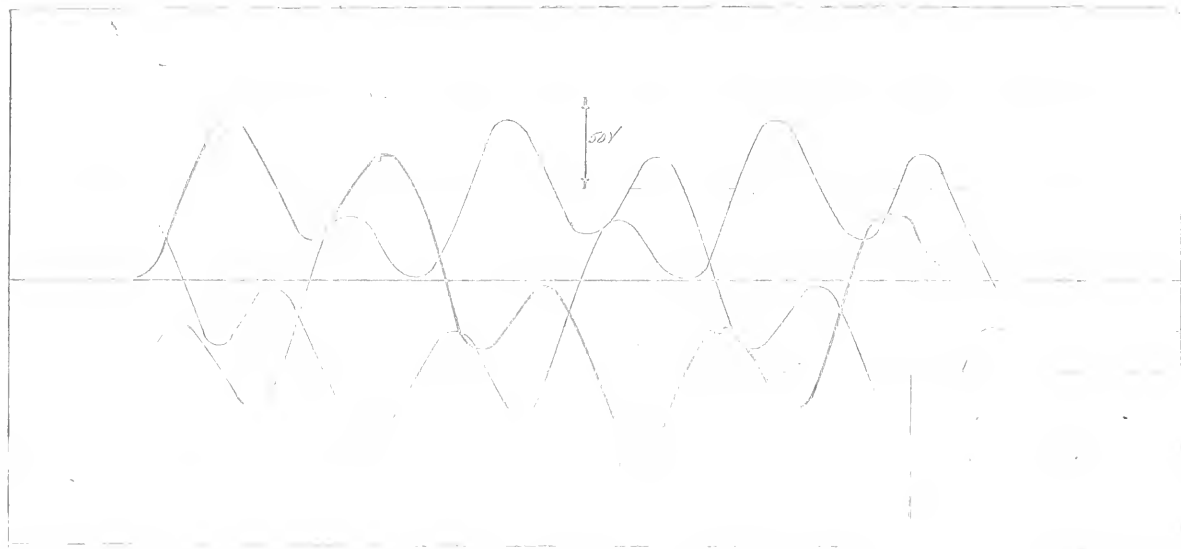
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the third harmonic. It is possible that some of the losses in 3 phase transforming apparatus may be due to the above mentioned losses of power and it is possible that this may be attributed a share of the "load losses" (Behrend p.27) of induction motors. 4 Six poles was the maximum of the three phase machines available with a maximum normal frequency of 60 cycles. Even if a 5 to 1 ratio of gears had been available to connect such a machine to the 500 revolution rotary furnishing the fundamental it would have been scarcely advisable to have run the 60 cycle machine at 2500 revolutions---more than twice its normal speed. A general electric induction motor class 4-10-750 form H (open rotor type) was available and it was coupled direct to the 75 cycle generator driven from the rotary shaft and run backwards at 1500 revolutions, its fields being excited from the 75 cycle current, giving 125 cycles at the rotor terminals. The motor was of but 20 H. P., but as the pressure required was low and a relatively high one could be produced in it, it was arranged to step down the pressure, thus decreasing the current necessary in the rotor to balance the line current. This was accomplished by a 3 phase and 3 single phase transformers as shown by Fig. 10. This gave the wave forms shown in curve B.

A practical objection to this scheme of series transformers arose from the fact that their inductances ~~were~~ exerted a depressing influence upon the 125 cycle peaks of the curve as shown by curves 3 and 4, showing the resultant of 65 V fundamental and 12 V harmonic with and without load. Little effect was noticed on the fundamental curves (curves 5 and 6).

To counteract this effect a synchronous motor and a power factor meter were put on the line as shown in Fig. 11, giving the complete and final scheme. The load and excitation of the synchronous motor were used to adjust the power factor, and curves 8 and 9 were made. A change in the wave form may still be noted, although the ratio of fundamental to harmonic has been unchanged.

Any reactance in the external circuit would affect the fundamental and the harmonic voltages in the ratio of their frequencies. Hence if one must be raised to keep the





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total voltage constant as a load comes on, if one other is raised proportionally in the ratio of their frequencies the greater effect of the external reactance on the harmonic should be overcome, and the wave form unchanged. For instance, if the ratio of fundamental to harmonic voltage be as 75 to 15, and the frequencies as 25 to 125, one volt rise of fundamental pressure would require $\frac{125}{25} \times \frac{15}{75} \times 1$ volt equal 1 volt rise

in harmonic pressure. This was tried and while with high external reactance (curve 10) it does not work very well, with a fair power factor the curve under load may be made to practically coincide with the no load curve (see curves 8 & 11).

PART II.

THE MOTOR TESTS.

The load curves of an induction motor cover most of the practical demands for information as to its performance. In addition to these the starting and accelerating characteristics, useful for some classes of work can best be determined from a series of speed curves, showing the relation of torque, current, power factor, etc. to speed or to slip.

The motor used was No. 31694 2-3 phase induction motor, General electric type 1 form K.L. (squirrel cage). Some of the principal dimensions of the machine are as follows:

Style I, Q 4-10-750.
Capacity, 10 P.
Number of poles, - 4,
Cycle speed 25/
R.P.M. 750,
Voltage (3 phase)-80

STATOR.

Circuits per phase 1,
Cond. in series per phase (3 phase) 1+4,
Size of conductors- 2- No.2 B.W.G.
Cond. per slot 6,
Slots 72,
Depth 1 1/4",
Width .335
Outside diam. punchings 21",
Inside diam. punchings, 15.7"
Air gap " - .33",
Length of punching 5".

ROTOR.

Winding, Squirrel cage,
#Slots, 47,
Size conductors .5" x .35",
Size slot 1 5/8" deep, 9/16" bottom 1/10" slit,
Outside diam. punchings- 15",
Inside diam. punching 11",
Area short circ. ring, .94 sq".
Length punching 5"

The following load curves show results of nine tests on as many wave forms:

Current Readings: The current input of the motor was read on Thomson O-200 ammeter No.24080 Previous to the test it was checked against electrogoniometer No.96 as follows:

Amperes.	Readings.	Amperes.	Readings.
22.8	22	48.6	50
32.8	33	59.6	60
39.5	40	62.0	62.2

For each load the meter was transferred by a special instrument switch to each of two phases and the average taken as the true current indication.

Power Readings: The kilowatt input of the motor was measured by the sum of the readings of Weston 0-100 amp. wattmeter No. 1778, when placed in each of two phases by the instrument transferring switch, the free pressure connection remaining on the third phase. Previous to the tests the meter was checked at a constant d.c. voltage of 100 as follows

True K.W.	Reading.	True K.W.	Reading.
1	1.04	7	7.00
2	2.04	8	8.04
3	3.04	9	9.00
4	4.04	10	10.10
5	5.05	11	10.97
6	6.06		

The power output was measured by a 13" prony brake of the band type operating on a steel pulley, water cooled. Readings were taken on a Fairbanks 0-525 lb. platform scale at a brake radius of 1.041 feet

Arrangements were made so that proper balance of the brake scales would light an incandescent lamp in front of the meter, insuring that readings be taken at correct balance.

Voltages: The motor voltage was kept constant at 80 by Weston 0-75-150 colymeter No. 753. The fundamental portion of this pressure was regulated by Thomson 0-130 voltmeter No. 6832 and the harmonic portion by Weston 0-15-25 voltmeter No. 3484.

Speed: All speed readings during the load runs were made with a totation counter and stop-watch. The generator cycle speed was regulated by No. 5217 Schaffner & Budenberg tachometer of the belt type. During the speed runs as mentioned later, Weston tachometer generator No. 18 was belted to the motor shaft and the speed calculated from the indications of No. 4401, Weston 0-3 voltmeter. The operation of these magnets speed indicators is too well known to require explanation.

Slip Measurement: The scheme of measuring the small slips incident to the load curves was as follows: A card was

mounted on the motor shaft at right angles thereto, bearing four spots, corresponding to the four poles of the generator, arranged in a circle and illuminated by a band feed arc lamp fed by same circuit as the motor. If the rotor was revolving at synchronism the spots would advance exactly one position in the half cycle corresponding to a period of comparative darkness of the lamp, and hence would appear stationary. But if the speed is less than synchronism each bright point of the lamp will find the spot a little farther back than before, of the position it would seem to occupy at synchronism. This results in a seeming ~~xxxxx~~ slow backward rotation of the spots at a speed equal to the slip.

It is of interest to note that when a flat wave was used the spots seemed to spread over quite a large surface, due to the long period of brightness, and that when a 2 or 3 peaked wave was used the spots appeared in twos or threes, due to periods of comparative darkness between peaks. This effect became so troublesome that the lamp was wired onto the sine portion of the wave by running its leads back to the machine generating the fundamental.

Slip measurements were made by timing the speed (R.P.M.) of these spots with a stop watch.

Tests: The load tests included readings of current, pressure, power and slip as various outputs, from which were calculated the torque, efficiency, power factor and apparent efficiency as shown by the following data and curves.

The power factor of the total current was maintained at unity by Westinghouse power factor meter No. 8960.

The speed curves: Considerable trouble was experienced before finding a good method of obtaining the torque, slip curves. It was impossible to merely load the motor until the slip reached the required amount, as the current, at full voltage would not only have been excessive even for short application, but the power factor of the total ~~xxxxxx~~ current could not have been maintained at the point necessary to preserve the wave form. (See part I.)

It was attempted to run the generators at low voltage, but it was found impossible in this case to keep the regulating synchronous motor on the line, and enough transformers were not available, either to step up the pressure to it, or to step it down to the induction motor.

The next scheme tried was a lowering of motor voltage by resistance in the form of lamp racks. While this gave the required pressure it was found impossible to keep it constant for any speed, the loss of voltage in it varying with the motor current, which in time varied with the slip so rapidly that when a given slip was reached the voltage would not ~~xxx~~ be correct and any attempt to change it would result in wide variations of speed.

The method as finally determined was this: The brake was removed and sufficient voltage was applied to the motor to keep it running, if started by hand, to overcome static friction. Readings of speed and current were then made and the torque and current calculated for full voltage at this slip, since the torque at any speed varies as the voltage squared and the current as the voltage. Readings for any other speed were taken by adjusting the voltage until the desired speed was reached and repeating the readings. The friction torque was assumed constant and if numerical results were desired instead of merely comparative ones, could have readily been determined. It was sufficient, however, to take this torque as unity, simplifying calculations. Care was taken that the speed was constant at the time of reading eliminating the torque of acceleration.

Current readings were made with Thomson O-100 ammeter No. 70184 and voltages with Weston O-15-25 voltmeter No. 3484.

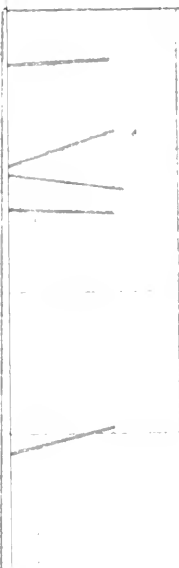
One curve only was obtained with the flat wave. As the thesis was at this point some weeks overdue we had to quit.

Wave No. 1

Wave No. 2

Wave No. 3





Ware №1.

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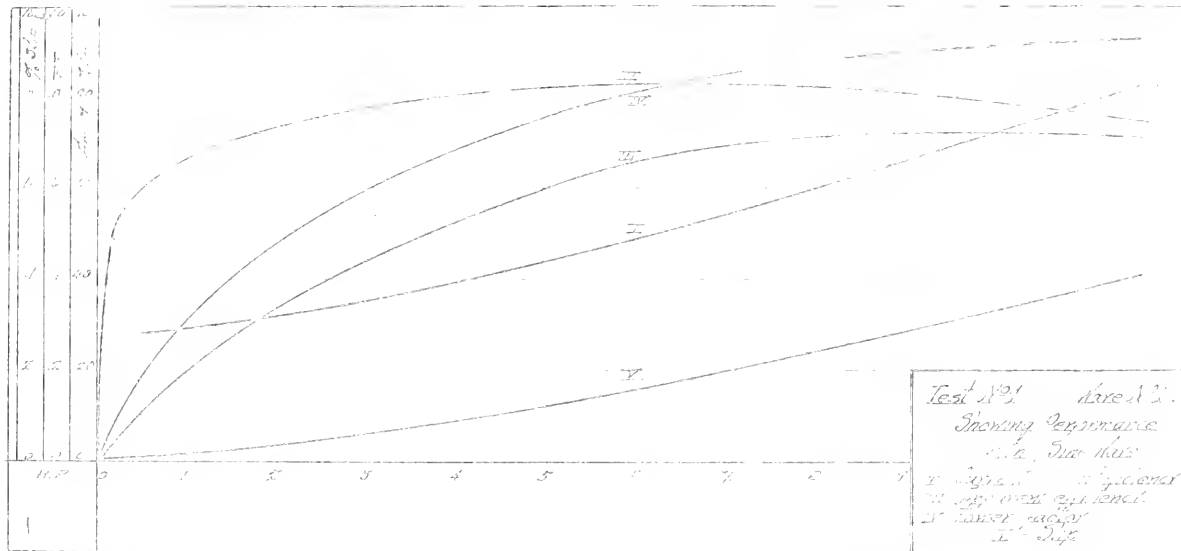
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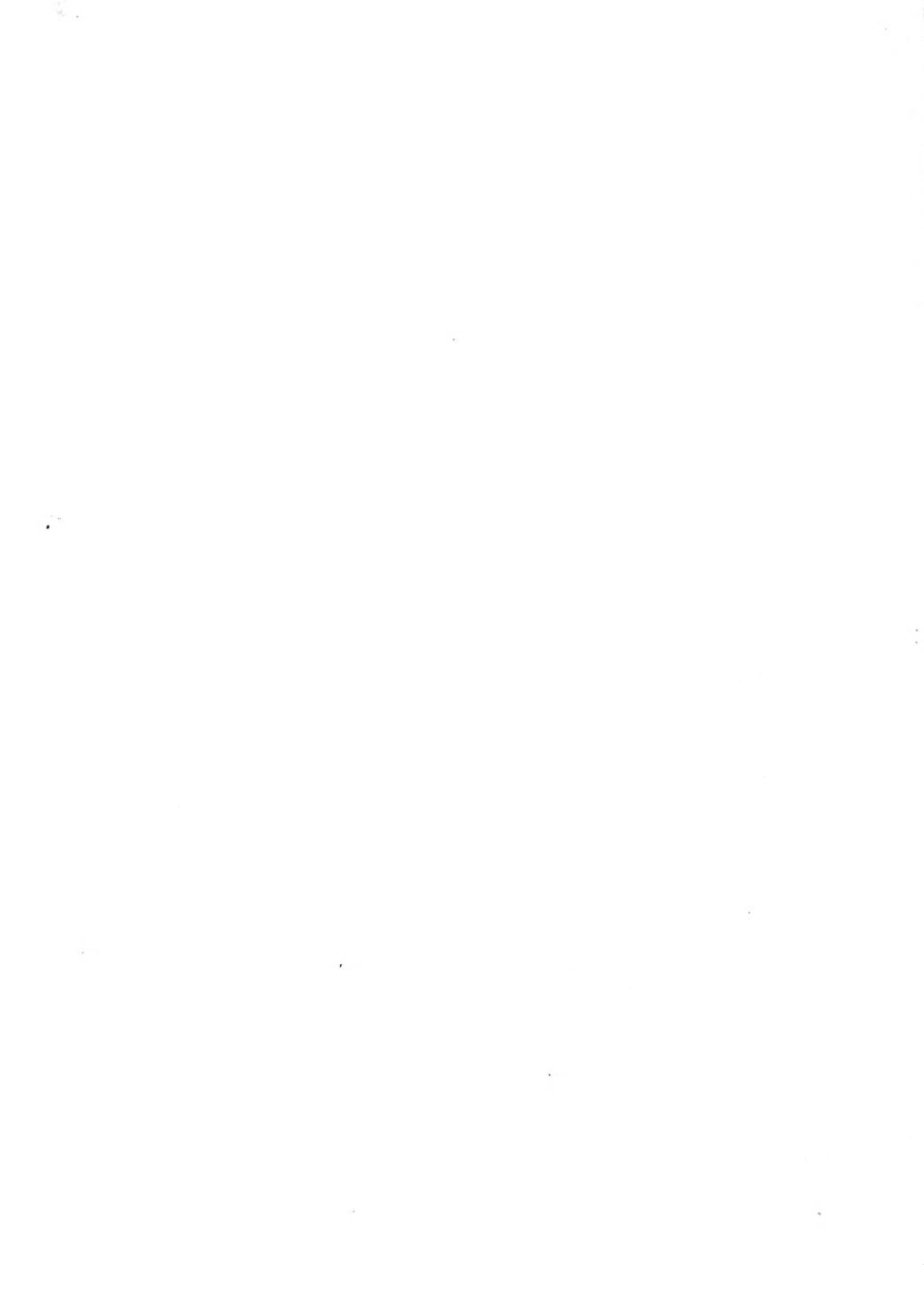
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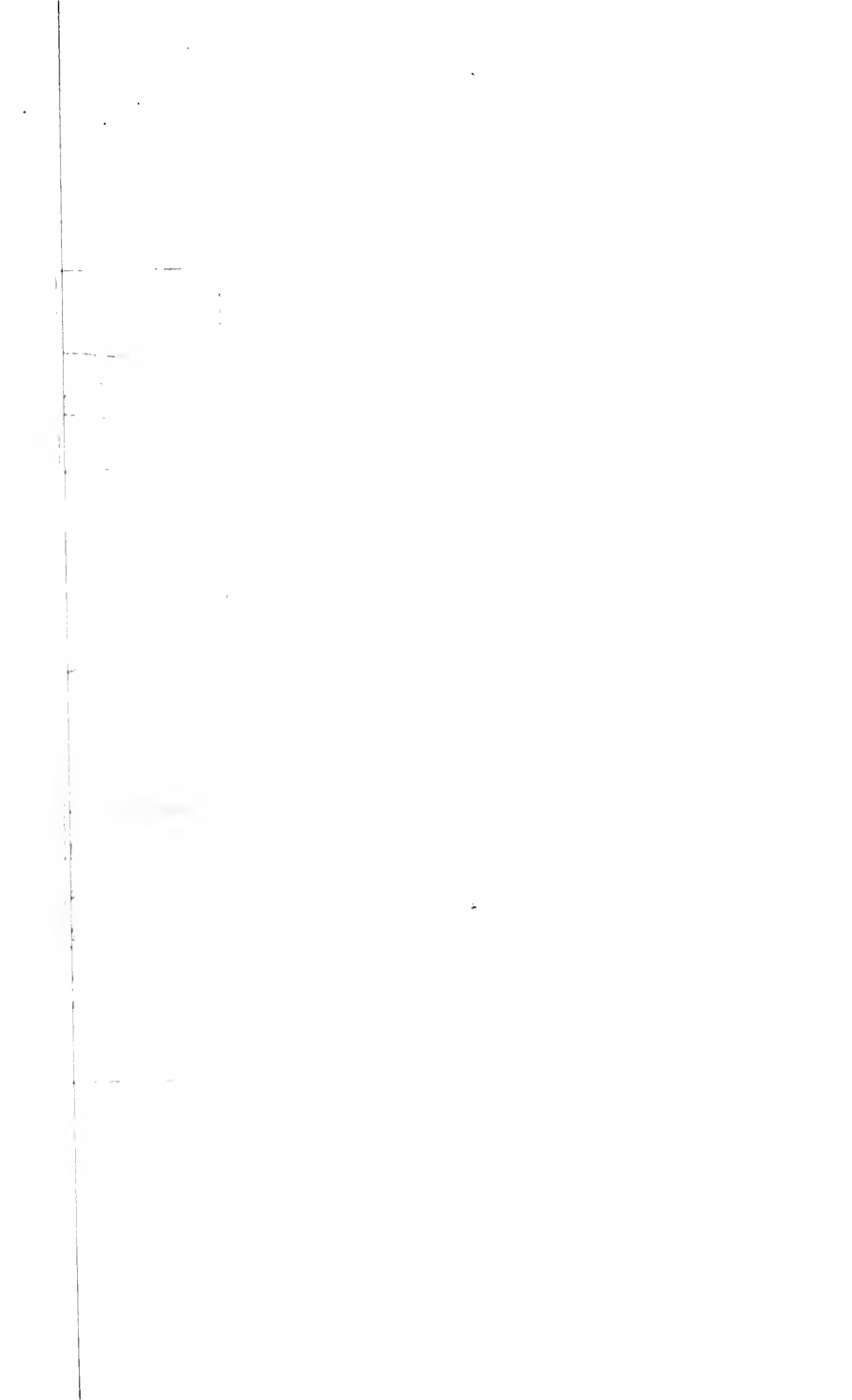
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TEST 1 Wave 10.1, 80 f. 35.5 slip, break radius, 1.41.

SLIP.	WAVE	LOS. OF RES.	WAVE CORRECTION	WAVE CORRECTION	S-P. CORRECTION	WAVE CORRECTION	WAVE CORRECTION	WAVE CORRECTION	SLIP
20.1	1.03	8.5	3.44	750	1.31	80.5	1.10	1.10	20.6
29.75	1.6	10.5	10.93	740	1.54	81.5	1.28	1.34	26.7
50.4	3.02	20.5	21.55	735	2.98	83.5	1.44	1.5	30.5
61.5	4.11	30.5	31.78	735	4.44	86.5	1.75	1.75	31.5
19	5.49	40.5	42.15	735	5.9	88.2	1.84	1.84	31.5
57.5	7.53	50.5	52.5	728	7.27	88.5	1.85	1.85	31.5
51.9	8.02	60.5	63.	731	8.76	91.5	1.82	1.82	31.5
72.7	9.11	70.5	73.45	730	10.2	93.5	1.85	1.85	31.5
82.5	10.33	80.5	83.7	725	11.58	94.5	1.82	1.82	31.5





3517 A. 1019 B. 25 Cycled 600 .

Amp.	W. Output Kw	W. Input Kw	Brake net. torque lb-ft	RPM	HP Output	HP Input	Eff. %	HP	Eff.
37.50	1.84	1.7	1.55	757	2.14	19.95	5.25	.102	.2
39	1.95	1.9	1.64	754	2.47	50.4	20.3	.361	.5
41.7	3.0	2.0	25.82	750	2.97	74.0	38.5	.52	.95
43.2	4.02	3.0	31.23	741	4.41	77.0	51.4	.609	1.40
53.1	5.18	4.0	41.64	745	5.9	80.5	60.0	.745	1.85
59.7	6.81	5.0	52.0	735	7.77	79.6	65.7	.825	2.5
65.2	7.97	6.0	62.40	732	8.65	81.5	72.0	.884	3.2
75.7	9.15	7.0	72.8	725	10.05	82.0	71.4	.897	3.7
87.2	10.82	8.0	83.8	720	11.41	85.5	70.1	.891	4.17
97.2	12.05	9.0	95.4	715	12.54	88.3	70.4	.894	5.0

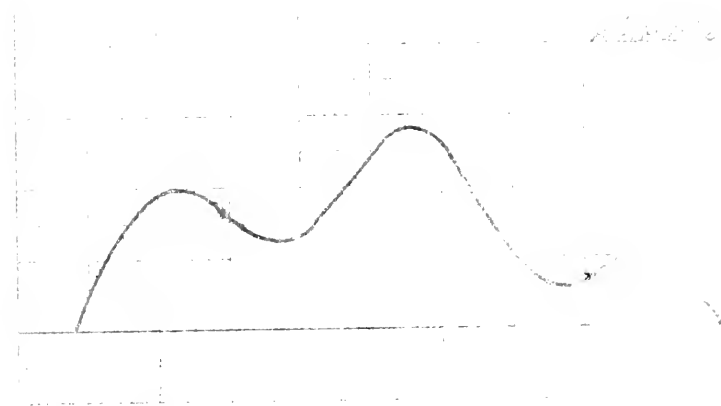
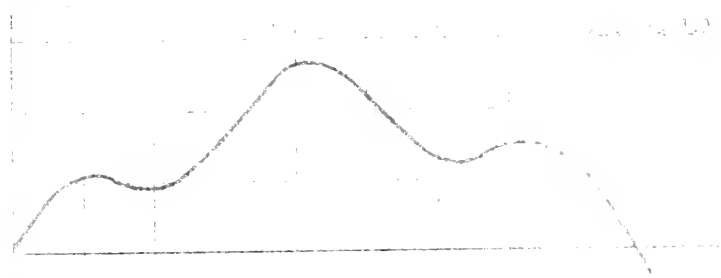
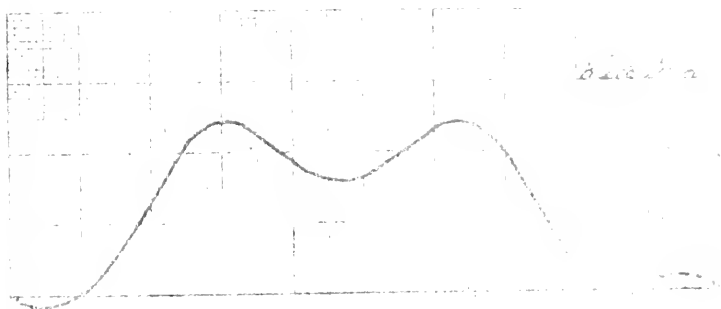






TEST NO. 1 Wave

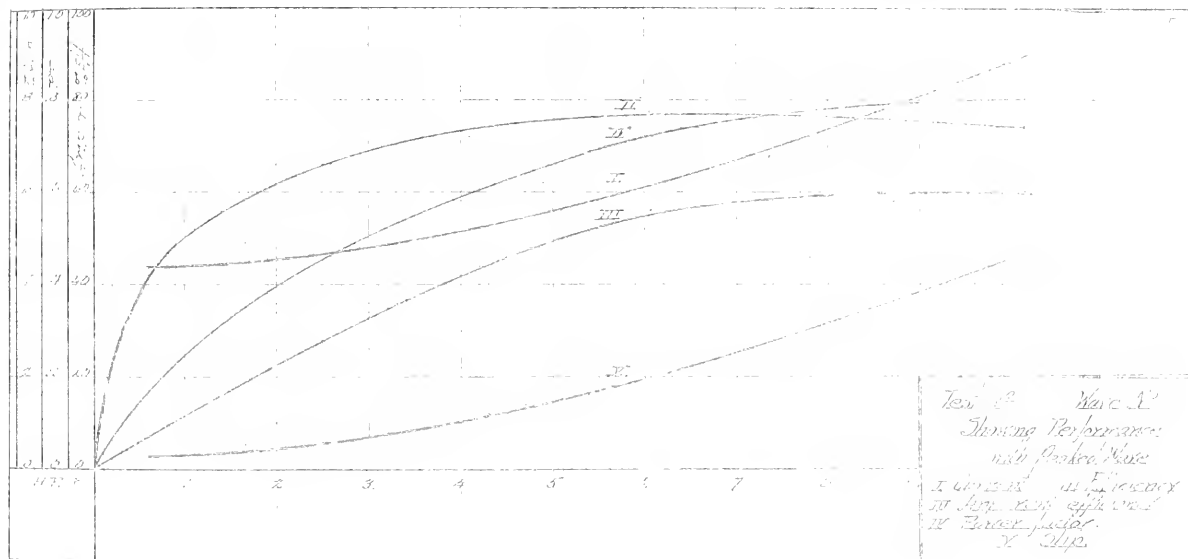
Amp.	Hz	Peak- to-Peak Volts	Frequency Kc	Imp. React.	Cap. React.	App. Res.	PF	Watt
33	1.09	10.25	31.1	7.0	1.51		.235	36
35.6	1.29	10.25	31.1	7.0	1.45	68.0	.354	1584
39.5	1.09	10.25	31.1	7.0	1.03	13.0	.569	.93
44.5	4.52	10.25	31.1	7.0	4.49	97.5	.701	1.4
52.3	5.43	10.25	31.1	7.0	5.34	51.5	.749	3.56
58.0	6.19	10.25	31.1	7.0	5.34	17.8	.801	3.1
67.5	7.87	10.25	31.1	7.0	1.88	63.5	.84	7.12
76.6	9.19	10.25	31.1	7.0	10.18	32.8	.874	3.1
87	10.52	10.25	31.1	7.0	11.15	21	.87	6.1
96.8	12.12	10.25	31.1	7.0	12.39	71.1	.885	11.1

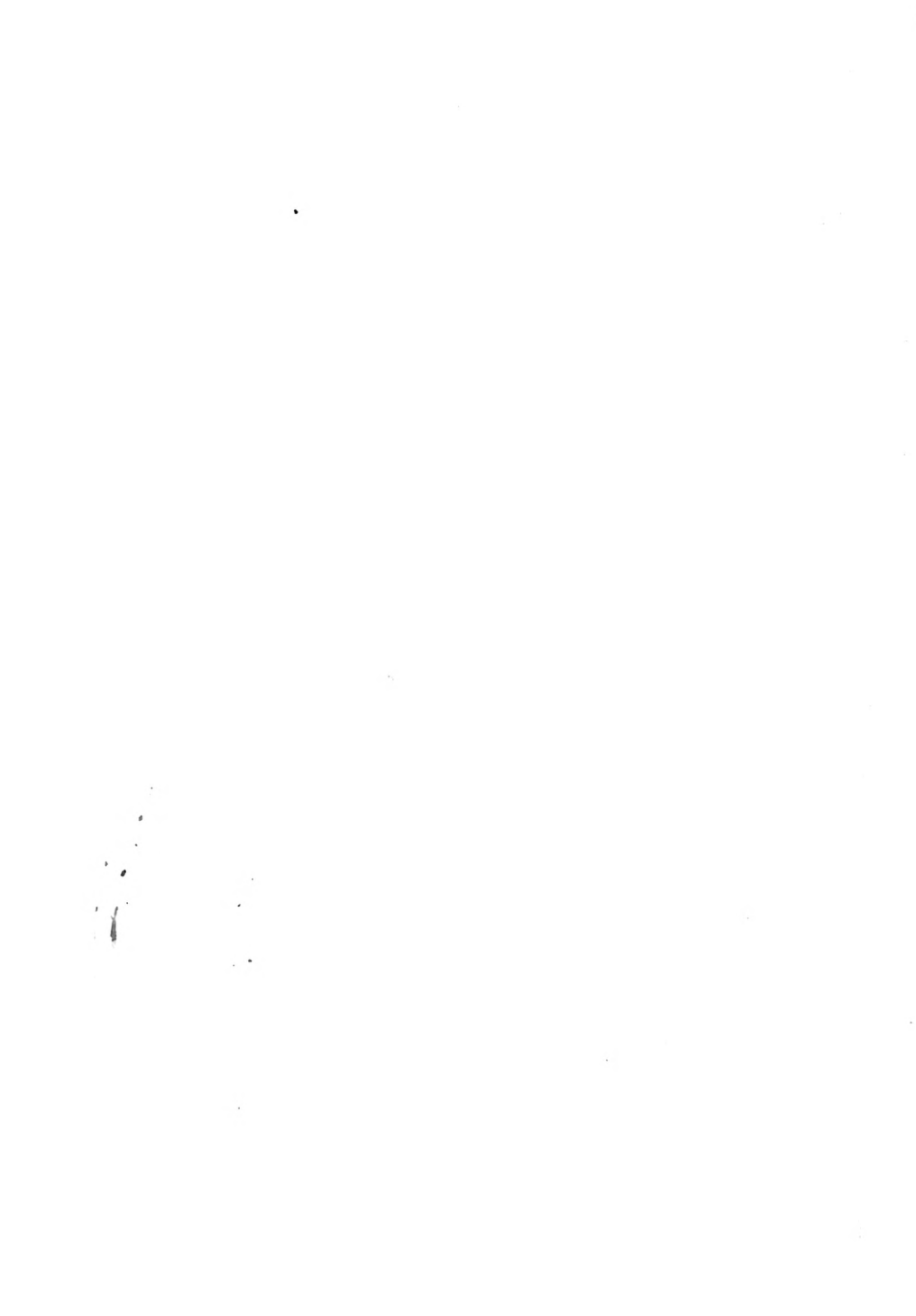


TEST NO. 4 Wave 4 25 Cycles 50 Volts, Brake Load 1.4

AMP.	WV	Dis. sec Brake.	Torque	RPM	HP Out- put	Eff. %	HP Inpt.	WV	Watt
54	3.35	8.25	8.5	55	1.04	59.8	1.74	1.294	1.01
58	3.4	13.75	14.00	58	1.07	62.9	21	.535	1.44
52	3.9	23.75	24.22	74.0	1.41	65.6	32.5	1.468	1.34
59	5.03	33.75	35.2	74.5	1.85	71.0	15.4	.535	2.0
72	5.0	43.75	43.7	780	6.35	57.3	40.5	1.905	2.38
77	6.1	53.75	55.5	785	7.52	50.9	53.9	1.96	1.35
84	6.4	63.75	64.3	720	9.08	78.0	33.5	1.91	1.01

<p> 1. Name 2. Address 3. City 4. State 5. Zip </p>





TEST NO. 3. Wires 8 35 37 38

Amp.	W	W ₂	W ₃	W ₄	W ₅	W ₆	W ₇
40	1.40	1.40	1.40	1.40	1.40	1.40	1.40
49	2.15	2.15	2.15	2.15	2.15	2.15	2.15
52	3.56	3.56	3.56	3.56	3.56	3.56	3.56
54.3	4.50	4.50	4.50	4.50	4.50	4.50	4.50
60	7.65	7.65	7.65	7.65	7.65	7.65	7.65
68.0	8.15	8.15	8.15	8.15	8.15	8.15	8.15
71	8.01	8.01	8.01	8.01	8.01	8.01	8.01
80.5	10.17	10.17	10.17	10.17	10.17	10.17	10.17

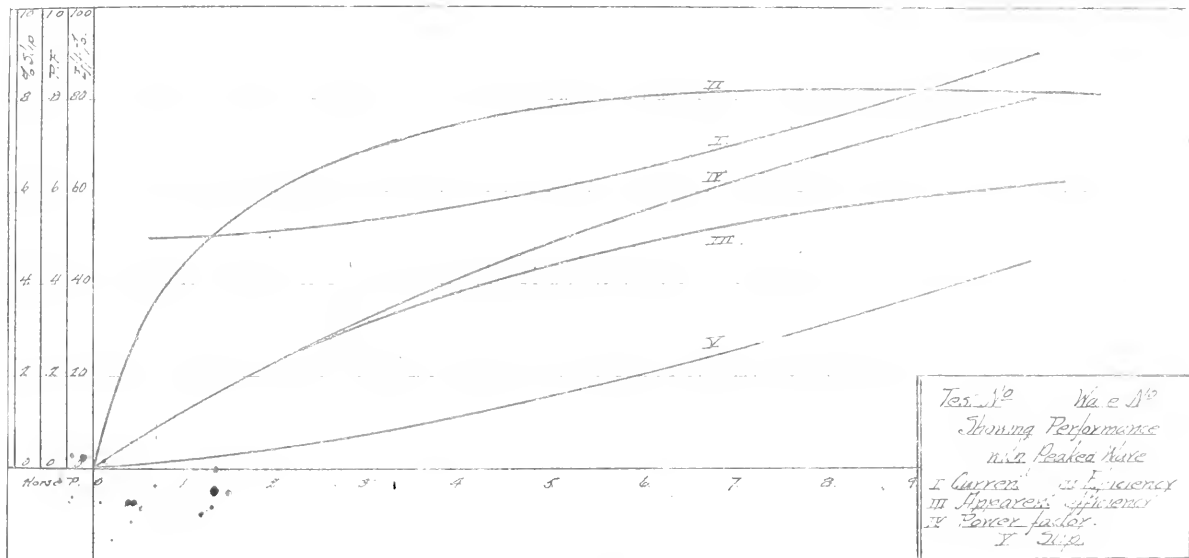
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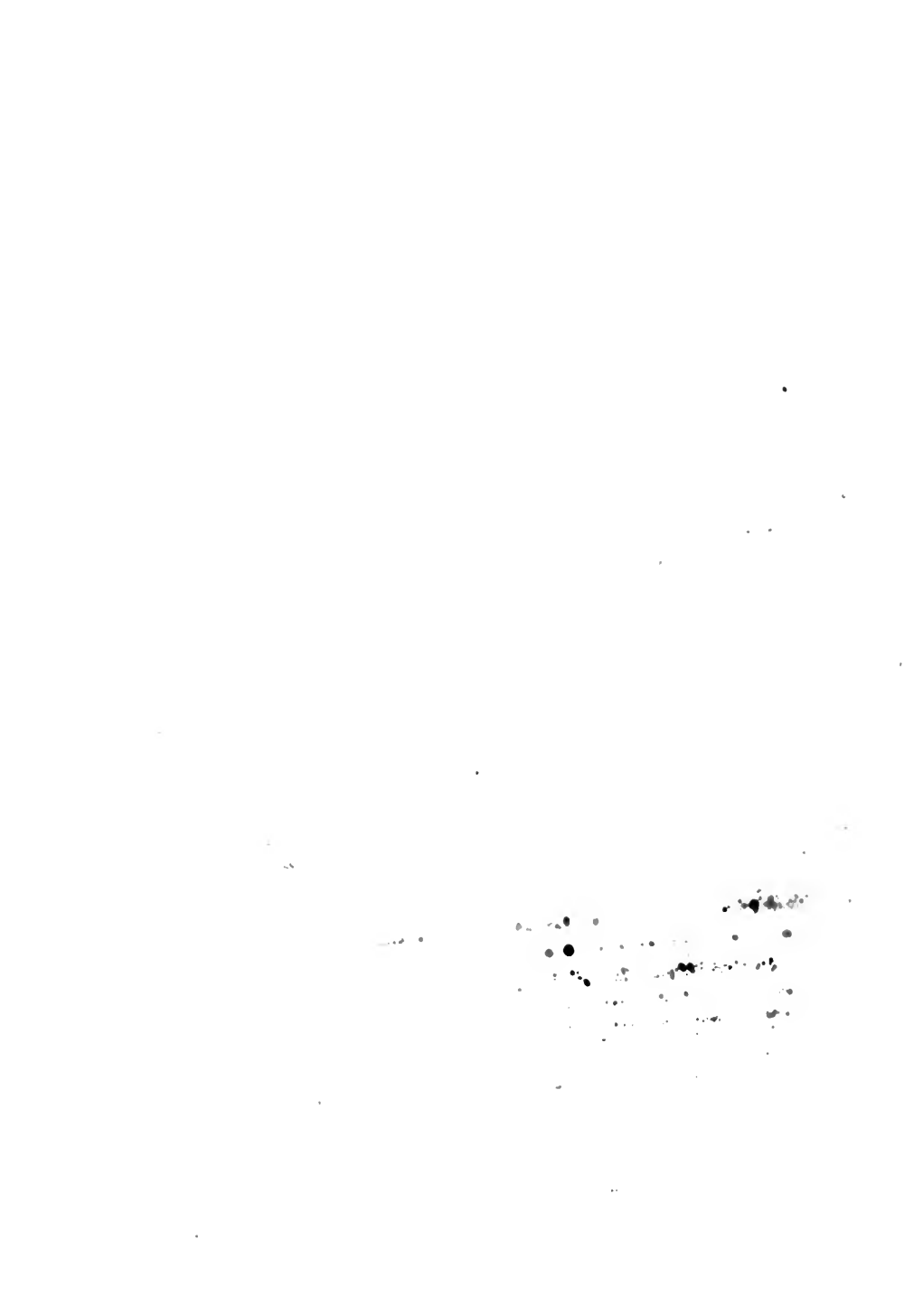
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Wave

Efficiency

efficiency.





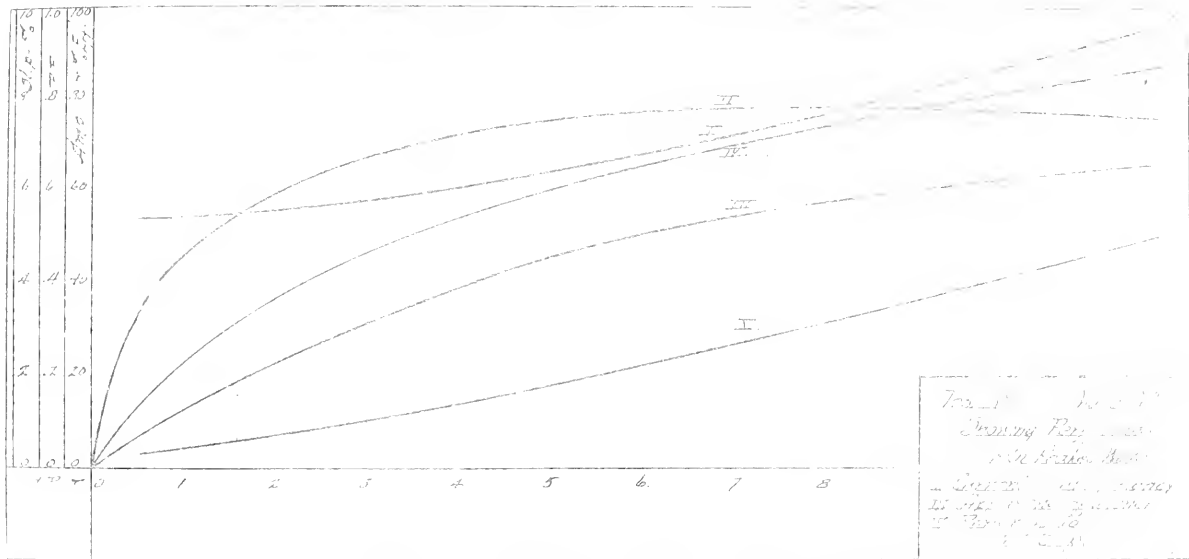
TEST NO. 6 Wave No. 6, 25 cycles, 80%, e.c.

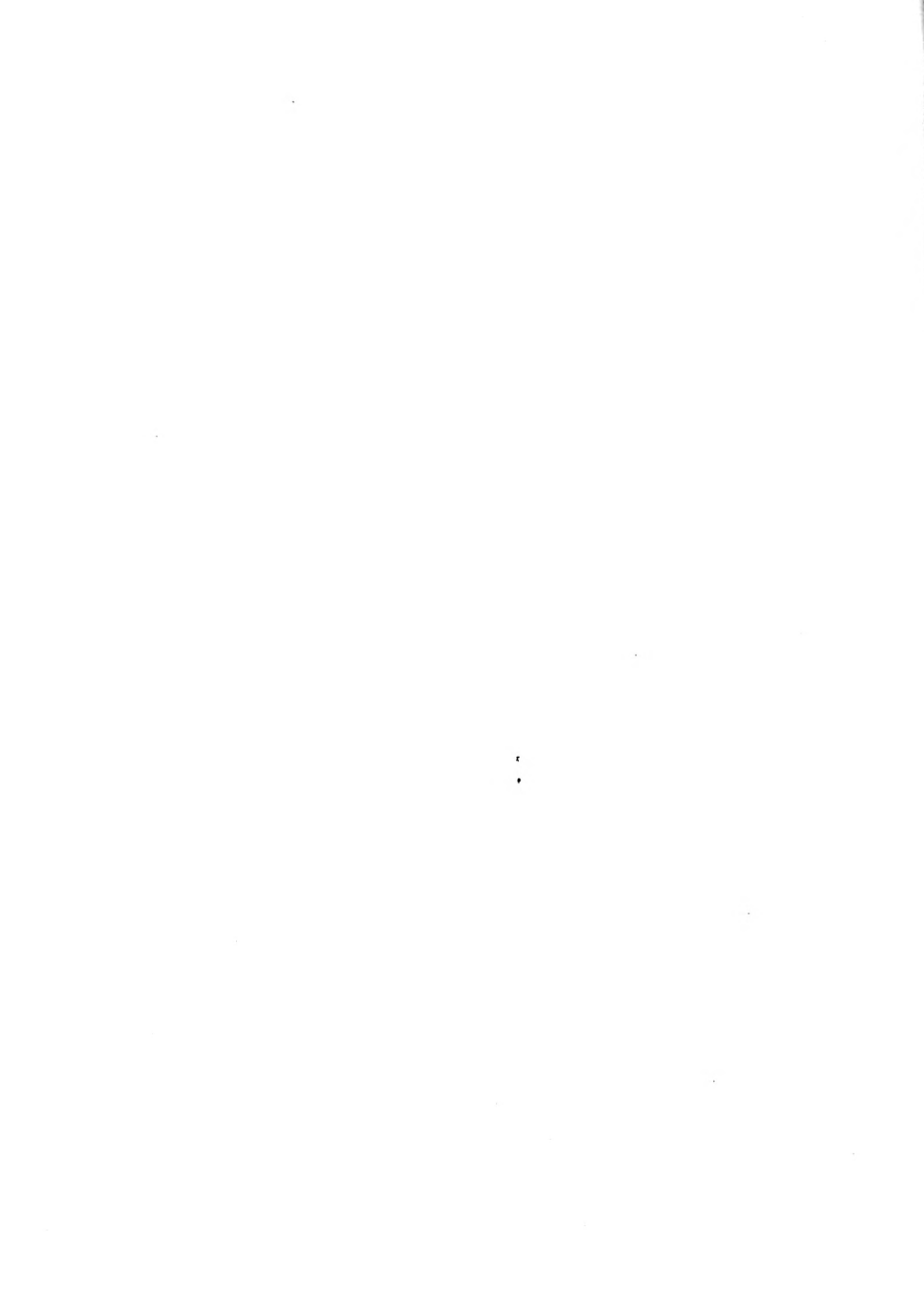
Amp.	AM	Pos. or Direct Ret.	Torque, RPM	H.P. output	Ref.	App. Eff.	FF	Slip %
50.6	1.4	4.5	4.68 747	.355	38.6	7.07	.198	.28
50	2.3	13	13.83 740	1.31	61.7	20.6	.332	.615
57	2.35	23	23.95 739	3.36	70.1	24	.342	1.2
59	4.3	33	34.35 735	4.8	74.6	26.2	.583	1.65
64.5	5.14	43	44.75 729	6.2	80	46.0	.575	2.11
73.8	6.53	53	55.2 725	7.6	86.6	58.3	.639	2.45
82	8.13	63	65.5 720	8.97	84.3	59	.713	3.37
90	10.13	73	75.0 715	10.0	75.2	61.7	.815	4.6



Date 11-2
 Name
 Wave
 Efficiency
 Density

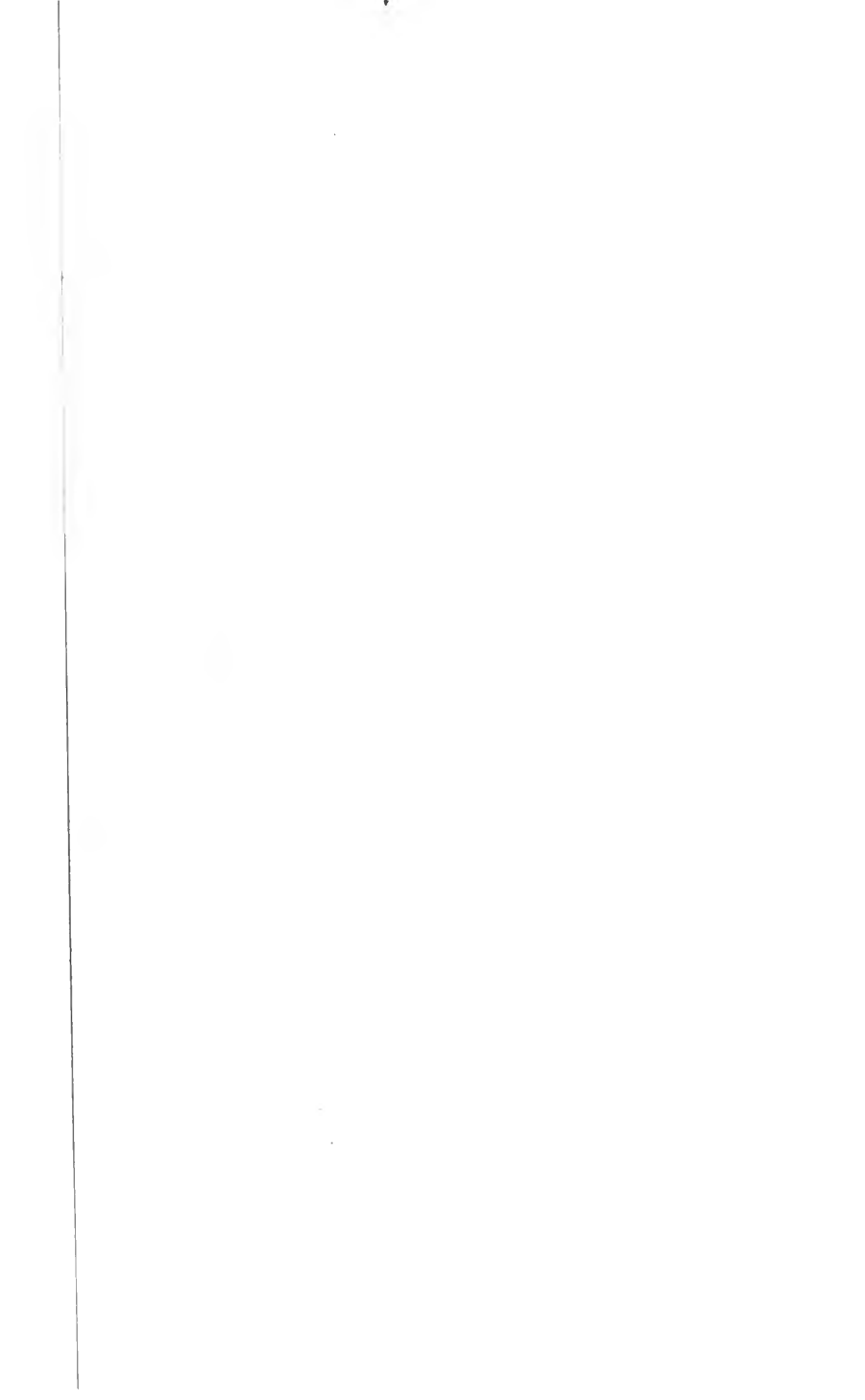






TEST NO. 5, 1-34-67, 21

Angle	W	Slope		S	T	V	H	L	1
		Per.	Feet						
50	1.1	3.15	3.55	0	1.1	1.1	1.1	1.1	1.25
56	2.12	11.25	11.55	11	1.1	11.2	11.2	11.2	1.64
62	3.1	21.25	21.25	12	1.1	21.0	21.0	21.0	1.91
69	4.65	31.25	31.25	13	1.1	31.7	31.7	31.7	1.27
66	4.90	41.25	41.25	136	1.1	41.7	41.7	41.7	2.16
72	5.15	51.25	51.2	148	1.1	51.2	51.2	51.2	3.02
74	6.13	61.25	61.25	124	1.1	61.2	61.2	61.2	1.17
87	11.12	71.25	71.2	120	1.1	71.2	71.2	71.2	4.16
96	11.32	81.25	81.2	110	1.1	81.2	81.2	81.2	4.06







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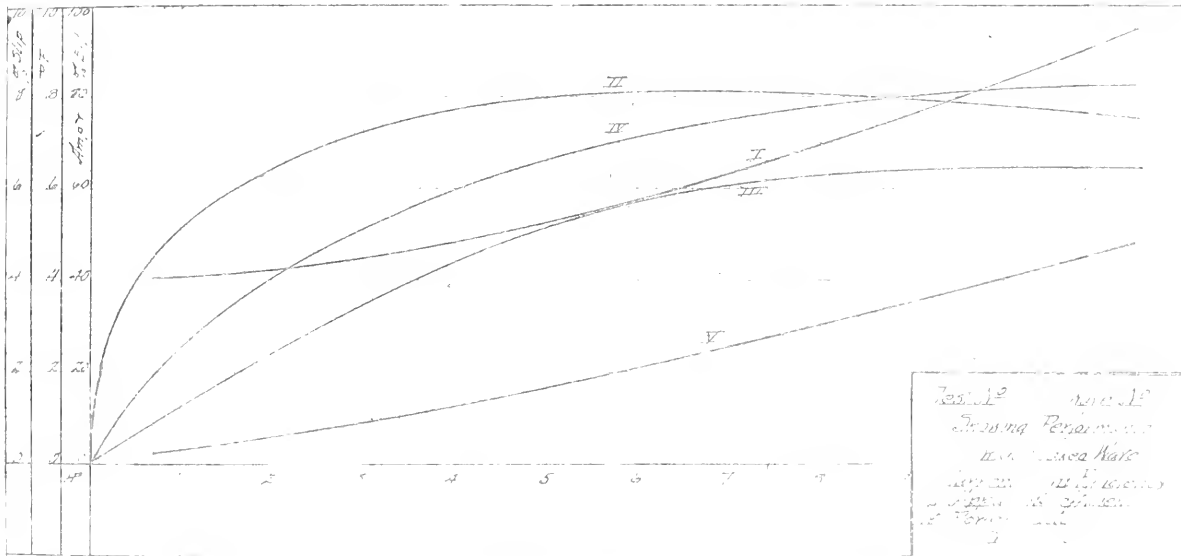




Table 1. The first 10 eigenvalues and eigenvectors of the covariance matrix of the 10 variables										
Order	Eigenvalue	Percentage of variance	Percentage of cumulative variance	1st	2nd	3rd	4th	5th	6th	7th
1	1.41	14.1%	14.1%	0.75	0.00	0.00	0.00	0.00	0.00	0.00
2	1.12	11.2%	25.3%	0.00	0.75	0.00	0.00	0.00	0.00	0.00
3	0.85	8.5%	33.8%	0.00	0.00	0.75	0.00	0.00	0.00	0.00
4	0.68	6.8%	40.6%	0.00	0.00	0.00	0.75	0.00	0.00	0.00
5	0.52	5.2%	45.8%	0.00	0.00	0.00	0.00	0.75	0.00	0.00
6	0.41	4.1%	49.9%	0.00	0.00	0.00	0.00	0.00	0.75	0.00
7	0.32	3.2%	53.1%	0.00	0.00	0.00	0.00	0.00	0.00	0.75
8	0.25	2.5%	55.6%	0.00	0.00	0.00	0.00	0.00	0.00	0.00
9	0.18	1.8%	57.4%	0.00	0.00	0.00	0.00	0.00	0.00	0.00
10	0.12	1.2%	58.6%	0.00	0.00	0.00	0.00	0.00	0.00	0.00



213.1-27
262
1000.

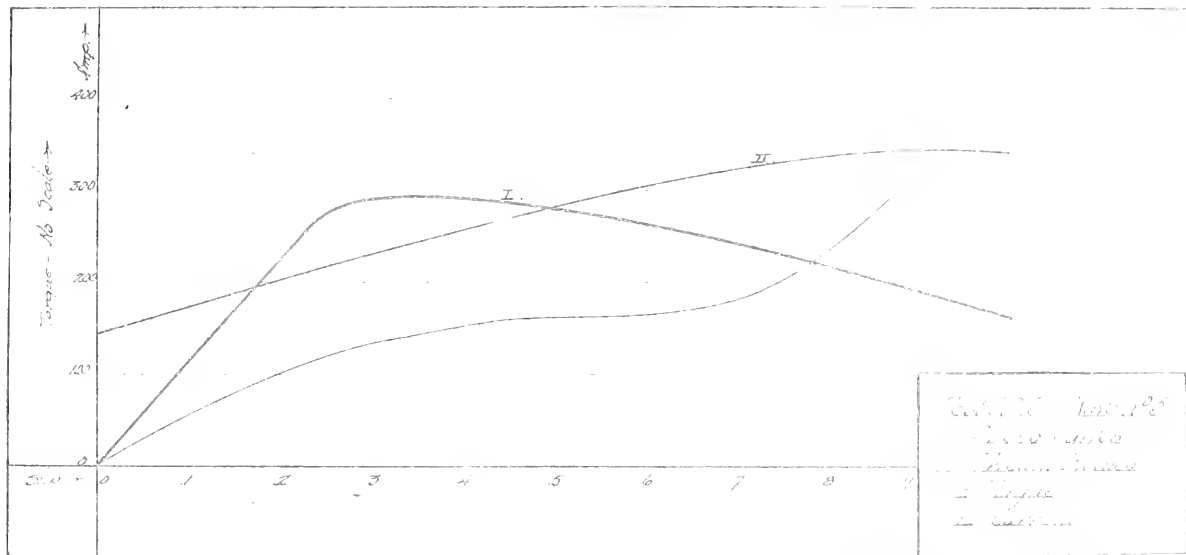


Table 1. *Mean values of the variables*

Year	Age	Sex	Height (cm)	Weight (kg)	Heart rate (b/min)
1997	20.0	50%	178	71.2	75
1998	20.1	50%	177	71	78
1999	20.2	50%	178	71	78
2000	20.3	50%	178	71	78
2001	20.4	50%	178	71	78
2002	20.5	50%	178	71	78
2003	20.6	50%	178	71	78
2004	20.7	50%	178	71	78
2005	20.8	50%	178	71	78
2006	20.9	50%	178	71	78
2007	21.0	50%	178	71	78
2008	21.1	50%	178	71	78
2009	21.2	50%	178	71	78
2010	21.3	50%	178	71	78
2011	21.4	50%	178	71	78
2012	21.5	50%	178	71	78
2013	21.6	50%	178	71	78
2014	21.7	50%	178	71	78
2015	21.8	50%	178	71	78
2016	21.9	50%	178	71	78
2017	22.0	50%	178	71	78
2018	22.1	50%	178	71	78
2019	22.2	50%	178	71	78
2020	22.3	50%	178	71	78
2021	22.4	50%	178	71	78
2022	22.5	50%	178	71	78
2023	22.6	50%	178	71	78
2024	22.7	50%	178	71	78
2025	22.8	50%	178	71	78
2026	22.9	50%	178	71	78
2027	23.0	50%	178	71	78
2028	23.1	50%	178	71	78
2029	23.2	50%	178	71	78
2030	23.3	50%	178	71	78
2031	23.4	50%	178	71	78
2032	23.5	50%	178	71	78
2033	23.6	50%	178	71	78
2034	23.7	50%	178	71	78
2035	23.8	50%	178	71	78
2036	23.9	50%	178	71	78
2037	24.0	50%	178	71	78
2038	24.1	50%	178	71	78
2039	24.2	50%	178	71	78
2040	24.3	50%	178	71	78
2041	24.4	50%	178	71	78
2042	24.5	50%	178	71	78
2043	24.6	50%	178	71	78
2044	24.7	50%	178	71	78
2045	24.8	50%	178	71	78
2046	24.9	50%	178	71	78
2047	25.0	50%	178	71	78
2048	25.1	50%	178	71	78
2049	25.2	50%	178	71	78
2050	25.3	50%	178	71	78
2051	25.4	50%	178	71	78
2052	25.5	50%	178	71	78
2053	25.6	50%	178	71	78
2054	25.7	50%	178	71	78
2055	25.8	50%	178	71	78
2056	25.9	50%	178	71	78
2057	26.0	50%	178	71	78
2058	26.1	50%	178	71	78
2059	26.2	50%	178	71	78
2060	26.3	50%	178	71	78
2061	26.4	50%	178	71	78
2062	26.5	50%	178	71	78
2063	26.6	50%	178	71	78
2064	26.7	50%	178	71	78
2065	26.8	50%	178	71	78
2066	26.9	50%	178	71	78
2067	27.0	50%	178	71	78
2068	27.1	50%	178	71	78
2069	27.2	50%	178	71	78
2070	27.3	50%	178	71	78
2071	27.4	50%	178	71	78
2072	27.5	50%	178	71	78
2073	27.6	50%	178	71	78
2074	27.7	50%	178	71	78
2075	27.8	50%	178	71	78
2076	27.9	50%	178	71	78
2077	28.0	50%	178	71	78
2078	28.1	50%	178	71	78
2079	28.2	50%	178	71	78
2080	28.3	50%	178	71	78
2081	28.4	50%	178	71	78
2082	28.5	50%	178	71	78
2083	28.6	50%	178	71	78
2084	28.7	50%	178	71	78
2085	28.8	50%	178	71	78
2086	28.9	50%	178	71	78
2087	29.0	50%	178	71	78
2088	29.1	50%	178	71	78
2089	29.2	50%	178	71	78
2090	29.3	50%	178	71	78
2091	29.4	50%	178	71	78
2092	29.5	50%	178	71	78
2093	29.6	50%	178	71	78
2094	29.7	50%	178	71	78
2095	29.8	50%	178	71	78
2096	29.9	50%	178	71	78
2097	30.0	50%	178	71	78
2098	30.1	50%	178	71	78
2099	30.2	50%	178	71	78
2100	30.3	50%	178	71	78
2101	30.4	50%	178	71	78
2102	30.5	50%	178	71	78
2103	30.6	50%	178	71	78
2104	30.7	50%	178	71	78
2105	30.8	50%	178	71	78
2106	30.9	50%	178	71	78
2107	31.0	50%	178	71	78
2108	31.1	50%	178	71	78
2109	31.2	50%	178	71	78
2110	31.3	50%	178	71	78
2111	31.4	50%	178	71	78
2112	31.5	50%	178	71	78
2113	31.6	50%	178	71	78
2114	31.7	50%	178	71	78
2115	31.8	50%	178	71	78
2116	31.9	50%	178	71	78
2117	32.0	50%	178	71	78
2118	32.1	50%	178	71	78
2119	32.2	50%	178	71	78
2120	32.3	50%	178	71	78
2121	32.4	50%	178	71	78
2122	32.5	50%	178	71	78
2123	32.6	50%	178	71	78
2124	32.7	50%	178	71	78
2125	32.8	50%	178	71	78
2126	32.9	50%	178	71	78
2127	33.0	50%	178	71	78
2128	33.1	50%	178	71	78
2129	33.2	50%	178	71	78
2130	33.3	50%	178	71	78
2131	33.4	50%	178	71	78
2132	33.5	50%	178	71	78
2133	33.6	50%	178	71	78
2134	33.7	50%	178	71	78
2135	33.8	50%	178	71	78
2136	33.9	50%	178	71	78
2137	34.0	50%	178	71	78
2138	34.1	50%	178	71	78
2139	34.2	50%	178	71	78
2140	34.3	50%	178	71	78
2141	34.4	50%	178	71	78
2142	34.5	50%	178	71	78
2143	34.6	50%	178	71	78
2144	34.7	50%	178	71	78
2145	34.8	50%	178	71	78
2146	34.9	50%	178	71	78
2147	35.0	50%	178	71	78
2148	35.1	50%	178	71	78
2149	35.2	50%	178	71	78
2150	35.3	50%	178	71	78
2151	35.4	50%	178	71	78
2152	35.5	50%	178	71	78
2153	35.6	50%	178	71	78
2154	35.7	50%	178	71	78
2155	35.8	50%	178	71	78
2156	35.9	50%	178	71	78
2157	36.0	50%	178	71	78
2158	36.1	50%	178	71	78
2159	36.2	50%	178	71	78
2160	36.3	50%	178	71	78
2161	36.4	50%	178	71	78
2162	36.5	50%	178	71	78
2163	36.6	50%	178	71	78
2164	36.7	50%	178	71	78
2165	36.8	50%	178	71	78
2166	36.9	50%	178	71	78
2167	37.0	50%	178	71	78
2168	37.1	50%	178	71	78
2169	37.2	50%	178	71	78
2170	37.3	50%	178	71	78
2171	37.4	50%	178	71	78
2172	37.5	50%	178	71	78
2173	37.6	50%	178	71	78
2174	37.7	50%	178	71	78
2175	37.8	50%	178	71	78
2176	37.9	50%	178	71	78
2177	38.0	50%	178	71	78
2178	38.1	50%	178	71	78
2179	38.2	50%	178	71	78
2180	38.3	50%	178	71	78
2181	38.4	50%	178	71	78
2182	38.5	50%	178	71	78
2183	38.6	50%	178	71	78
2184	38.7	50%	178	71	78
2185	38.8	50%	178	71	78
2186	38.9	50%	178	71	78
2187	39.0	50%	178	71	78
2188	39.1	50%	178	71	78
2189	39.2	50%	178	71	78
2190	39.3	50%	178	71	78
2191	39.4	50%	178	71	78
2192	39.5	50%	178	71	78
2193	39.6	50%	178	71	78
2194	39.7	50%	178	71	78
2195	39.8	50%	178	71	78
2196	39.9	50%	178	71	78
2197	40.0	50%	178	71	78
2198	40.1	50%	178	71	78
2199	40.2	50%	178	71	78
2200	40.3	50%	178	71	78
2201	40.4	50%	178	71	78
2202	40.5	50%	178	71	78
2203	40.6	50%	178	71	78
2204	40.7	50%	178	71	78
2205	40.8	50%	178	71	78
2206	40.9	50%	178	71	78
2207	41.0	50%	178	71	78
2208	41.1	50%	178	71	78
2209	41.2	50%	178	71	78
2210	41.3	50%	178	71	78
2211	41.4	50%	178	71	78
2212	41.5	50%	178	71	78
2213	41.6	50%	178	71	78
2214	41.7	50%	178	71	78
2215	41.8	50%	178	71	78
2216	41.9	50%	178	71	78
2217	42.0	50%	178	71	78
2218	42.1	50%	178	71	78
2219	42.2	50%	178	71	78
2220	42.3	50%	178	71	78
2221	42.4	50%	178	71	78
2222	42.5	50%	178	71	78
2223	42.6	50%	178	71	78
2224	42.7	50%	178	71	78
2225	42.8	50%	178	71	78
2226	42.9	50%	178	71	78
2227	43.0	50%	178	71	78
2228					



